

**GENERATING PARTIALS FOR PERSPECTIVE CORRECTED TEXTURE  
COORDINATES IN A FOUR PIXEL TEXTURE PIPELINE**

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**BACKGROUND OF THE INVENTION**

**1. Technical Field:**

The present invention relates to computer graphics.  
10 More specifically, the present invention relates to the  
selection of pixel density and image texture.

**2. Description of Related Art:**

In computer graphics, the purpose of determining  
15 partials is to find the rate of change inside the texture  
map with respect to the current pixel being processed.  
Partials are the partial derivatives of the texture  
coordinates with respect to the screen coordinates. A  
texture map is an image stored in memory that is applied  
20 on a per-pixel basis to rendered primitives (graphics  
elements that are used as building blocks for creating  
images, such as a point, line, arc, cone or sphere).  
These partials are used to pick a Level of Detail (LOD)  
which has the closest rate of change to one.

25 Triangle partials are used by the rasterizing  
hardware to step in the x and y direction to render  
pixels to the frame buffer. Perspective correction  
generates nonlinear changes across the texture map so  
that the resulting image is in accordance to the view  
30 point being rendered. Normally the partials match the  
triangle partials, but if the texture coordinates are  
perspective corrected this is not true and the hardware

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has to perform a calculation on a per pixel basis to find the true partial.

Therefore, it would be desirable to have a method for generating partials for perspective corrected texture  
5 coordinates which requires fewer multiplies than the traditional method of calculating the partials for each pixel separately.

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**SUMMARY OF THE INVENTION**

The present invention provides a method, program and  
5 apparatus for generating partial differential equations  
for perspective corrected texture coordinates in a  
computer graphics display. The present invention  
comprises calculating texture coordinates for four  
adjacent pixels and then determining the differences  
10 between the coordinates. A perspective correction factor  
is then calculated, which is multiplied by each  
coordinate difference.

**BRIEF DESCRIPTION OF THE DRAWINGS**

The novel features believed characteristic of the invention are set forth in the appended claims. The invention itself, however, as well as a preferred mode of use, further objectives and advantages thereof, will best be understood by reference to the following detailed description of an illustrative embodiment when read in conjunction with the accompanying drawings, wherein:

**Figure 1** depicts a pictorial representation of a data processing system in which the present invention may be implemented;

**Figure 2** depicts a block diagram of a data processing system in which the present invention may be implemented;

**Figure 3** depicts a schematic diagram illustrating an arrangement of pixels in accordance with the present invention;

**Figure 4** depicts a schematic diagram illustrating the definition of the deltas for adjacent pixels in accordance with the present invention;

**Figure 5** depicts a schematic diagram illustrating a hardware implementation for the partials in accordance with the present invention; and

**Figure 6** depicts a flowchart illustrating the process of hardware implementation for the partials in accordance with the present invention.

**DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT**

With reference now to the figures and in particular  
5 with reference to **Figure 1**, a pictorial representation of  
a data processing system in which the present invention  
may be implemented is depicted in accordance with a  
preferred embodiment of the present invention. A  
computer **100** is depicted which includes a system unit  
10 **110**, a video display terminal **102**, a keyboard **104**,  
storage devices **108**, which may include floppy drives and  
other types of permanent and removable storage media, and  
mouse **106**. Additional input devices may be included with  
personal computer **100**, such as, for example, a joystick,  
15 touchpad, touch screen, trackball, microphone, and the  
like. Computer **100** can be implemented using any suitable  
computer, such as an IBM RS/6000 computer or  
IntelliStation computer, which are products of  
International Business Machines Corporation, located in  
20 Armonk, New York. Although the depicted representation  
shows a computer, other embodiments of the present  
invention may be implemented in other types of data  
processing systems, such as a network computer. Computer  
**100** also preferably includes a graphical user interface  
25 that may be implemented by means of systems software  
residing in computer readable media in operation within  
computer **100**.

With reference now to **Figure 2**, a block diagram of a  
data processing system is shown in which the present  
30 invention may be implemented. Data processing system **200**  
is an example of a computer, such as computer **100** in

**Figure 1**, in which code or instructions implementing the processes of the present invention may be located. Data processing system **200** employs a peripheral component interconnect (PCI) local bus architecture. Although the depicted example employs a PCI bus, other bus architectures such as Accelerated Graphics Port (AGP) and Industry Standard Architecture (ISA) may be used. Processor **202** and main memory **204** are connected to PCI local bus **206** through PCI bridge **208**. PCI bridge **208** also may include an integrated memory controller and cache memory for processor **202**. Additional connections to PCI local bus **206** may be made through direct component interconnection or through add-in boards. In the depicted example, local area network (LAN) adapter **210**, small computer system interface SCSI host bus adapter **212**, and expansion bus interface **214** are connected to PCI local bus **206** by direct component connection. In contrast, audio adapter **216**, graphics adapter **218**, and audio/video adapter **219** are connected to PCI local bus **206** by add-in boards inserted into expansion slots. Expansion bus interface **214** provides a connection for a keyboard and mouse adapter **220**, modem **222**, and additional memory **224**. SCSI host bus adapter **212** provides a connection for hard disk drive **226**, tape drive **228**, and CD-ROM drive **230**. Typical PCI local bus implementations will support three or four PCI expansion slots or add-in connectors.

An operating system runs on processor **202** and is used to coordinate and provide control of various components within data processing system **200** in **Figure 2**. The operating system may be a commercially available operating system such as Windows 2000, which is available from

Microsoft Corporation. An object oriented programming system such as Java may run in conjunction with the operating system and provides calls to the operating system from Java programs or applications executing on data processing system 200. "Java" is a trademark of Sun Microsystems, Inc. Instructions for the operating system, the object-oriented programming system, and applications or programs are located on storage devices, such as hard disk drive 226, and may be loaded into main memory 204 for execution by processor 202.

Those of ordinary skill in the art will appreciate that the hardware in **Figure 2** may vary depending on the implementation. Other internal hardware or peripheral devices, such as flash ROM (or equivalent nonvolatile memory) or optical disk drives and the like, may be used in addition to or in place of the hardware depicted in **Figure 2**. Also, the processes of the present invention may be applied to a multiprocessor data processing system.

For example, data processing system 200, if optionally configured as a network computer, may not include SCSI host bus adapter 212, hard disk drive 226, tape drive 228, and CD-ROM 230, as noted by dotted line 232 in **Figure 2** denoting optional inclusion. In that case, the computer, to be properly called a client computer, must include some type of network communication interface, such as LAN adapter 210, modem 222, or the like. As another example, data processing system 200 may be a stand-alone system configured to be bootable without relying on some type of network communication interface, whether or not data processing system 200 comprises some type of network communication interface. As a further

example, data processing system **200** may be a personal digital assistant (PDA), which is configured with ROM and/or flash ROM to provide non-volatile memory for storing operating system files and/or user-generated data.

The depicted example in **Figure 2** and above-described examples are not meant to imply architectural limitations. For example, data processing system **200** also may be a notebook computer or hand held computer in addition to taking the form of a PDA. Data processing system **200** also may be a kiosk or a Web appliance. The processes of the present invention are performed by processor **202** using computer implemented instructions, which may be located in a memory such as, for example, main memory **204**, memory **224**, or in one or more peripheral devices **226-230**. The present invention can be implemented in graphics adapter **218**.

It has become possible to process multiple texture pixels in a cycle with the advance of silicon technology. In a system that lights four texture pixels simultaneously, the partials can be calculated by taking the difference between the calculated texture coordinates at each of the four adjacent pixels and then multiplying each difference by a factor based on the perspective correction coordinate. This method requires fewer multiplies than the traditional method of calculating the partials for each pixel separately.

In the following description, the term "multiply" refers to the process of multiplication between numbers. In hardware, a multiply would be replaced with a multiplication unit (i.e. floating point or fixed point multiplication unit). The same applies to the terms



"subtracts" and "adds". These functions can be replaced by actual hardware units implementing the functions, or replaced in software with a line of code performing those functions.

5        S, T, R, and Q are texture coordinates that are sent at each vertex of a triangle to index into a texture map. S, T, R, and Q as capital letters refer to the non-perspective corrected coordinates.

10        The lower case s, t, r, and q are the perspective corrected version of the texture coordinates. They can be written as:

$$s = \frac{S}{Q} \quad \text{eq. 1}$$

15

$$t = \frac{T}{Q} \quad \text{eq. 2}$$

$$r = \frac{R}{Q} \quad \text{eq. 3}$$

20         $qr = \frac{1}{Q} \quad \text{eq. 4}$

25        The standard method for calculating the partials is derived by taking the partial derivative of the perspective corrected coordinate with respect to the screen coordinate or  $\frac{\partial s}{\partial x}$ .

Using eq. 1 this yields:

$$\frac{\partial s}{\partial x} = \frac{\partial}{\partial x} \left( \frac{S}{Q} \right) \quad \text{eq. 5}$$

30        Using the Quotient Rule of Derivatives:

$$\frac{\partial s}{\partial x} = \frac{Q \frac{\partial S}{\partial x} - S \frac{\partial Q}{\partial x}}{Q^2} \quad \text{eq. 6}$$

The partials on the right hand side of eq. 6 are the triangle partials of the non-perspective corrected texture coordinates. Eq. 6 can be reduced to:

5

$$\frac{\partial s}{\partial x} = \frac{1}{Q} \left( \frac{\partial S}{\partial x} - \frac{S}{Q} \frac{\partial Q}{\partial x} \right) \text{ eq. 7}$$

Substituting in eq. 1 and eq. 4 generates the standard equation:

10

$$\frac{\partial s}{\partial x} = qr \left( \frac{\partial S}{\partial x} - s \frac{\partial Q}{\partial x} \right) \text{ eq. 8}$$

Eq. 9 is what is typically implemented in hardware applications. There are two multiplies and one subtract per partial. The actual value needed is  $\frac{\partial u}{\partial x}$ , where u is an additional way for indexing the texture map that ranges from 0 to the width of the texture map vs. from 0 to 1 with s.

20

$$u = sw \quad \text{eq. 9 (where w is the width)}$$

Since w is constant across the texture map:

$$\frac{\partial u}{\partial x} = \frac{\partial s}{\partial x} w \quad \text{eq. 10}$$

25 This yields a final equation of:

$$\frac{\partial u}{\partial x} = qr \left( \frac{\partial S}{\partial x} - s \frac{\partial Q}{\partial x} \right) w \text{ eq. 11}$$

In some hardware systems the width, height and depth are restricted to values that are powers of two. In such a case, exponents can be added instead of doing a multiply. However, since more systems are moving to

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non-power-of-two textures, and because the present discussion is only concerned with the generic set of equations for calculating partials, the width factor will be treated as a multiply. This yields a total of 72  
 5 multiplies and 24 subtracts for calculating all the partials (3D included) for four pixels simultaneously.

Referring now to **Figure 3**, a schematic diagram illustrating an arrangement of pixels is depicted in accordance with the present invention. With a texture  
 10 engine that lights four pixels in a cycle, this new algorithm can be implemented. The pixels must be adjacent so that the deltas between x values and y values are always one. **Figure 3** shows the arrangement.

It should be noted that the subscripts on the  
 15 texture coordinates in the equations refer to the coordinates for the associated pixel in **Figure 3**.

If perspective correction is off, it makes sense that:

$$\frac{\partial u}{\partial x} = \frac{\Delta u}{\Delta x} \quad \text{eq. 12}$$

20

Since, for this case,  $\Delta x=1$ (see Fig. 1) this can be rewritten:

$$\frac{\Delta u}{\Delta x} = u_1 - u_0 \quad \text{eq. 13}$$

25 This, however, is not correct if the texture is perspective corrected. Again, since the width is constant:

$$\frac{\Delta u}{\Delta x} = (s_1 - s_0)w \quad \text{eq. 14}$$

30 Going back to eq. 1,  $s_1$  and  $s_0$  can be found as:

$$s_1 = \frac{s_1}{Q_1} \quad \text{eq. 15}$$

$$s_0 = \frac{s_0}{Q_0} \quad \text{eq. 16}$$

In the rasterizing process, subsequent coordinates are found by adding the partials in the given directions.

5 Therefore:

$$S_1 = S_0 + \frac{\partial S}{\partial x} \quad \text{eq. 17}$$

$$Q_1 = Q_0 + \frac{\partial Q}{\partial x} \quad \text{eq. 18}$$

10

Using eq. 14 the slope for s can be found.

$$\frac{\Delta s_0}{\Delta x} = \frac{S_0 + \frac{\partial S}{\partial x}}{Q_0 + \frac{\partial Q}{\partial x}} - \frac{S_0}{Q_0} \quad \text{eq. 19}$$

15 It is obvious that eq. 19 does not match eq. 8, but if the error between them can be found, a new solution for  $\frac{\partial u}{\partial x}$  can be generated using the error term. The error is:

$$\text{error} = \frac{\text{eq19} - \text{eq8}}{\text{eq8}} \quad \text{eq. 20}$$

20

or

$$\text{error} = \frac{\text{eq19}}{\text{eq8}} - 1 \quad \text{eq. 21}$$

25 Substituting the error into the equation produces the following equation:

$$\text{error} = \frac{\frac{S_0 + \frac{\partial S}{\partial x}}{Q_0 + \frac{\partial Q}{\partial x}} - \frac{S_0}{Q_0}}{\frac{1}{Q_0} \left( \frac{\partial S}{\partial x} - \frac{S_0}{Q_0} \frac{\partial Q}{\partial x} \right)} - 1 \quad \text{eq. 22}$$

Reduction of eq. 22:

$$\frac{Q_0 \left[ \frac{s_0 + \frac{\partial s}{\partial x}}{Q_0 + \frac{\partial Q}{\partial x}} \right]}{\frac{\partial s}{\partial x} - \frac{s_0}{Q_0} \frac{\partial Q}{\partial x}} - \left[ \frac{s_0}{\frac{\partial s}{\partial x} - \frac{s_0}{Q_0} \frac{\partial Q}{\partial x}} - 1 \right]$$

$$5 \quad \frac{Q_0 \left( \frac{s_0 + \frac{\partial s}{\partial x}}{Q_0 + \frac{\partial Q}{\partial x}} \right) - s_0}{\frac{\partial s}{\partial x} - \frac{s_0}{Q_0} \frac{\partial Q}{\partial x}} - 1$$

$$\frac{\frac{Q_0 s_0}{Q_0 + \frac{\partial Q}{\partial x}} - \left( \frac{Q_0 \frac{\partial s}{\partial x}}{Q_0 + \frac{\partial Q}{\partial x}} - \left( \frac{Q_0 s_0}{Q_0 + \frac{\partial Q}{\partial x}} - \frac{s_0 \frac{\partial Q}{\partial x}}{Q_0 + \frac{\partial Q}{\partial x}} \right) \right)}{\frac{\partial s}{\partial x} - \frac{s_0}{Q_0} \frac{\partial Q}{\partial x}} - 1$$

$$\frac{\frac{Q_0 \frac{\partial s}{\partial x} - s_0 \frac{\partial Q}{\partial x}}{Q_0 + \frac{\partial Q}{\partial x}}}{\left( Q_0 \frac{\partial s}{\partial x} - s_0 \frac{\partial Q}{\partial x} \right) \frac{1}{Q_0}} - 1$$

10

$$\frac{Q_0 \frac{\partial s}{\partial x} - s_0 \frac{\partial Q}{\partial x}}{Q_0 + \frac{\partial Q}{\partial x}} \frac{Q_0}{Q_0 \frac{\partial s}{\partial x} - s_0 \frac{\partial Q}{\partial x}} - 1$$

$$\text{error} = \frac{Q_0}{Q_0 + \frac{\partial Q}{\partial x}} - 1 \text{ eq. 23}$$

15 It should be noted that the form of this equation matches the original error equation (eq. 21). Setting them equal produces:

$$\frac{Q_0}{Q_0 + \frac{\partial Q}{\partial x}} - 1 = \frac{\frac{\Delta s_0}{\Delta x}}{\frac{\partial s_0}{\partial x}} - 1 \quad \text{eq. 24}$$

20

Therefore:

$$\frac{\partial s_0}{\partial x} = \frac{\Delta s_0}{\Delta x} \left( \frac{Q_0 + \frac{\partial Q}{\partial x}}{Q_0} \right) \quad \text{eq. 25}$$

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Substituting eq. 18 into eq. 25:

$$\frac{\partial s_0}{\partial x} = \frac{\Delta s_0}{\Delta x} \left( \frac{Q_1}{Q_0} \right) \quad \text{eq. 26}$$

5 or

$$\frac{\partial s_0}{\partial x} = \frac{\Delta s_0}{\Delta x} q_1 q r_0 \quad \text{eq. 27}$$

10 Since, ultimately,  $\frac{\partial u}{\partial x}$  is being sought, the equations 10 and 14 can be used to substitute in and rewrite equation 27 in terms of  $\frac{\partial u}{\partial x}$ , which yields equation 28:

$$\frac{\partial u_0}{\partial x} = \frac{\Delta u_0}{\Delta x} q_1 q r_0 \quad \text{eq. 28}$$

15 Equation 28 has one subtract and two multiplies per partial. Each partial can be derived similarly to eq. 28. In total, this yields 48 multiplies versus 72 multiplies for the standard equations.

Referring to **Figure 4**, a schematic diagram  
 20 illustrating the definition of the deltas for adjacent pixels is depicted in accordance with the present invention. To define the rest of the partials all of the deltas for a group of four adjacent pixels must first be defined. Each number in **Figure 4** represents a texture  
 25 coordinate (u). **Figure 4** defines the differences between  $u_0$  and  $u_1$ , divided by the change in x as  $\frac{\Delta u_0}{\Delta x}$ . The same applies to the other changes depicted in **Figure 4**.  $\frac{\Delta u_1}{\Delta y}$  is defined as the difference between  $u_1$  and  $u_3$ , divided by the change in y. As the change in x and change in y are  
 30 always one (the pixels are adjacent), **Figure 4** defines equations 29 through 32.

Equations 29 through 32 show the equations for each of the deltas.

$$\begin{array}{ll} \frac{\Delta u_0}{\Delta x} = u_1 - u_0 & \text{eq. 29} \\ 5 \quad \frac{\Delta u_2}{\Delta x} = u_3 - u_2 & \text{eq. 30} \\ \frac{\Delta u_0}{\Delta y} = u_2 - u_0 & \text{eq. 31} \\ \frac{\Delta u_1}{\Delta y} = u_3 - u_1 & \text{eq. 32} \end{array}$$

From similar derivations of equation 28 the following set of equations (33 to 40) can be found. These equations describe how u is moving for all four pixels. The equations for the other texture components v and w are found exactly the same as u. Substitute v and w wherever there is a u produces the v and w equations.

$$\begin{array}{ll} 15 \quad \frac{\partial u_0}{\partial x} = \frac{\Delta u_0}{\Delta x} q_1 q r_0 & \text{eq. 33} \\ \frac{\partial u_1}{\partial x} = \frac{\Delta u_0}{\Delta x} q_0 q r_1 & \text{eq. 34} \\ 20 \quad \frac{\partial u_2}{\partial x} = \frac{\Delta u_2}{\Delta x} q_3 q r_2 & \text{eq. 35} \\ \frac{\partial u_3}{\partial x} = \frac{\Delta u_2}{\Delta x} q_2 q r_3 & \text{eq. 36} \\ \frac{\partial u_0}{\partial y} = \frac{\Delta u_0}{\Delta y} q_2 q r_0 & \text{eq. 37} \\ 25 \quad \frac{\partial u_1}{\partial y} = \frac{\Delta u_1}{\Delta y} q_3 q r_1 & \text{eq. 38} \\ \frac{\partial u_2}{\partial y} = \frac{\Delta u_0}{\Delta y} q_0 q r_2 & \text{eq. 39} \\ 30 \quad \frac{\partial u_3}{\partial y} = \frac{\Delta u_1}{\Delta y} q_1 q r_3 & \text{eq. 40} \end{array}$$

In the next equation for v0 the delta is also multiplied by q1qr0:

$$35 \quad \frac{\partial v_0}{\partial x} = \frac{\Delta v_0}{\Delta x} q_1 q r_0 \quad \text{eq. 41}$$

This holds true for all the partials of u, v and w. This means that in a hardware application eight factors can be

calculated that each of the deltas can be multiplied by correspondingly to get the final results.

The final algorithm in equation form (eq. 42 to 73) is presented below. The algorithm uses 12 subtracts and  
 5 32 multiplies, versus the 24 subtracts and 72 multiplies of the standard algorithm in the prior art.

The factors:

$$f_{x_0} = q_1 q r_0 \quad \text{eq. 42}$$

$$10 \quad f_{x_1} = q_0 q r_1 \quad \text{eq. 43}$$

$$f_{x_2} = q_3 q r_2 \quad \text{eq. 44}$$

$$15 \quad f_{x_3} = q_2 q r_3 \quad \text{eq. 45}$$

$$f_{y_0} = q_2 q r_0 \quad \text{eq. 46}$$

$$f_{y_1} = q_3 q r_1 \quad \text{eq. 47}$$

$$20 \quad f_{y_2} = q_0 q r_2 \quad \text{eq. 48}$$

$$f_{y_3} = q_1 q r_3 \quad \text{eq. 49}$$

The partials:

25

$$\frac{\partial u_0}{\partial x} = \frac{\Delta u_0}{\Delta x} f_{x_0} \quad \text{eq. 50}$$

$$\frac{\partial u_0}{\partial y} = \frac{\Delta u_0}{\Delta y} f_{y_0} \quad \text{eq. 51}$$

$$30 \quad \frac{\partial v_0}{\partial x} = \frac{\Delta v_0}{\Delta x} f_{x_0} \quad \text{eq. 52}$$



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$$\frac{\partial v_0}{\partial y} = \frac{\Delta v_0}{\Delta y} f_{y_0} \quad \text{eq. 53}$$

$$\frac{\partial w_0}{\partial x} = \frac{\Delta w_0}{\Delta x} f_{x_0} \quad \text{eq. 54}$$

$$5 \quad \frac{\partial w_0}{\partial y} = \frac{\Delta w_0}{\Delta y} f_{y_0} \quad \text{eq. 55}$$

$$\frac{\partial u_1}{\partial x} = \frac{\Delta u_0}{\Delta x} f_{x_1} \quad \text{eq. 56}$$

$$10 \quad \frac{\partial u_1}{\partial y} = \frac{\Delta u_1}{\Delta y} f_{y_1} \quad \text{eq. 57}$$

$$\frac{\partial v_1}{\partial x} = \frac{\Delta v_0}{\Delta x} f_{x_1} \quad \text{eq. 58}$$

$$\frac{\partial v_1}{\partial y} = \frac{\Delta v_1}{\Delta y} f_{y_1} \quad \text{eq. 59}$$

$$15 \quad \frac{\partial w_1}{\partial x} = \frac{\Delta w_0}{\Delta x} f_{x_1} \quad \text{eq. 60}$$

$$\frac{\partial w_1}{\partial y} = \frac{\Delta w_1}{\Delta y} f_{y_1} \quad \text{eq. 61}$$

$$\frac{\partial u_2}{\partial x} = \frac{\Delta u_2}{\Delta x} f_{x_2} \quad \text{eq. 62}$$

$$20 \quad \frac{\partial u_2}{\partial y} = \frac{\Delta u_0}{\Delta y} f_{y_2} \quad \text{eq. 63}$$

$$\frac{\partial v_2}{\partial x} = \frac{\Delta v_2}{\Delta x} f_{x_2} \quad \text{eq. 64}$$

$$25 \quad \frac{\partial v_2}{\partial y} = \frac{\Delta v_0}{\Delta y} f_{y_2} \quad \text{eq. 65}$$

$$\frac{\partial w_2}{\partial x} = \frac{\Delta w_2}{\Delta x} f_{x_2} \quad \text{eq. 66}$$

$$\frac{\partial w_2}{\partial y} = \frac{\Delta w_0}{\Delta y} f_{y_2} \quad \text{eq. 67}$$

$$\frac{\partial u_3}{\partial x} = \frac{\Delta u_2}{\Delta x} f_{x_3} \quad \text{eq. 68}$$

$$\frac{\partial u_3}{\partial y} = \frac{\Delta u_1}{\Delta y} f_{y_3} \quad \text{eq. 69}$$

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$$\frac{\partial v_3}{\partial x} = \frac{\Delta v_2}{\Delta x} f_{x_3} \quad \text{eq. 70}$$

$$\frac{\partial v_3}{\partial y} = \frac{\Delta v_1}{\Delta y} f_{y_3} \quad \text{eq. 71}$$

$$10 \quad \frac{\partial w_3}{\partial x} = \frac{\Delta w_2}{\Delta x} f_{x_3} \quad \text{eq. 72}$$

$$\frac{\partial w_3}{\partial y} = \frac{\Delta w_1}{\Delta y} f_{y_3} \quad \text{eq. 73}$$

15 Referring now to **Figure 5**, a schematic diagram illustrating a hardware implementation for the partials is depicted in accordance with the present invention. The present system can be implemented by a series of subtracts and multiplies. The subtracts and first stage  
20 of multiplies can be done in parallel. The second stage contains only the remaining multiplies. The entire figure represents the hardware implementation of equations 33 through 40 and shows the number of multiplies and subtracts necessary for calculating the  
25 partials of the texture coordinate u for four pixels.

Referring to **Figure 6**, a flowchart illustrating the process of hardware implementation for the partials is depicted in accordance with the present invention. The process flow begins by calculating the deltas (step **601**).  
30 This process uses a set of subtracts in parallel to create the deltas defined by equations 29 through 32.

Next, the correction factors are calculated (step **602**). The correction factors are a set of multipliers that take the incoming perspective coordinates and generate the factors that will be multiplied by the deltas (equations 5 42 through 49). In hardware, this occurs in parallel with the subtraction calculations for the deltas (they are not dependent upon each other). After the correction factors are calculated, they are then multiplied by the deltas to obtain the true partials (step **603**).

10 It is important to note that while the present invention has been described in the context of a fully functioning data processing system, those of ordinary skill in the art will appreciate that the processes of the present invention are capable of being distributed in 15 the form of a computer readable medium of instructions and a variety of forms and that the present invention applies equally regardless of the particular type of signal bearing media actually used to carry out the distribution. Examples of computer readable media 20 include recordable-type media, such as a floppy disk, a hard disk drive, a RAM, CD-ROMs, DVD-ROMs, and transmission-type media, such as digital and analog communications links, wired or wireless communications links using transmission forms, such as, for example, 25 radio frequency and light wave transmissions. The computer readable media may take the form of coded formats that are decoded for actual use in a particular data processing system.

The description of the present invention has been 30 presented for purposes of illustration and description, and is not intended to be exhaustive or limited to the invention in the form disclosed. Many modifications and

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variations will be apparent to those of ordinary skill in the art. The embodiment was chosen and described in order to best explain the principles of the invention, the practical application, and to enable others of  
5 ordinary skill in the art to understand the invention for various embodiments with various modifications as are suited to the particular use contemplated.